

***Many Body Effects in Carbon Nanotube
Fluorescence Spectroscopy***

E.J. Mele and C.L. Kane

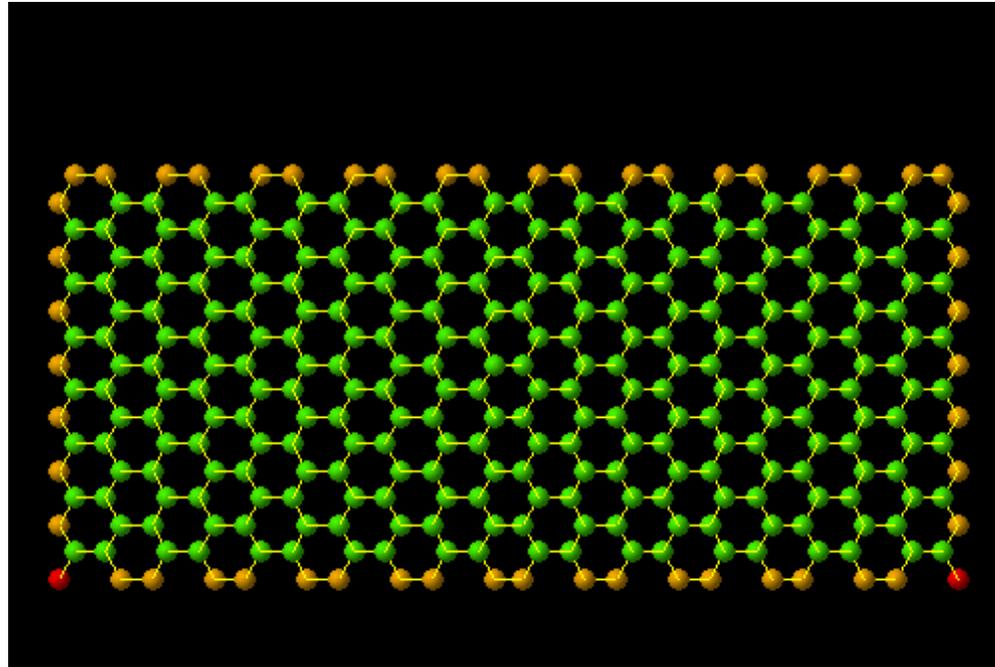
Sheets and Cylinders of Graphene

Photophysics of NT's (mainly exptl)

***Scaling Relations in Optical Properties
from e-e Interactions***



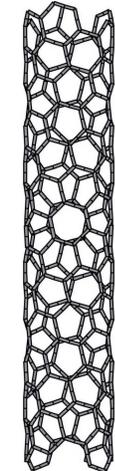
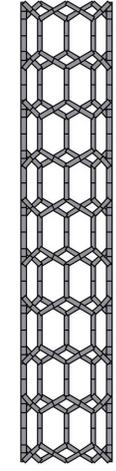
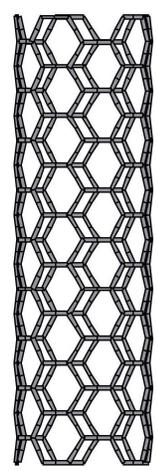
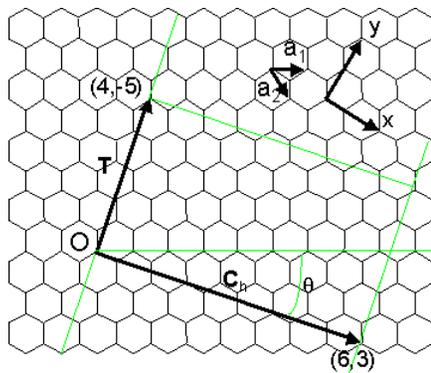
Nanotubes from wrapped graphene



Each tube is indexed by the translation vector around its circumference

NT as a molecule, a 1D wire, a quantum dot, a semiconductor, an interconnect...

Rolling-up a graphene sheet

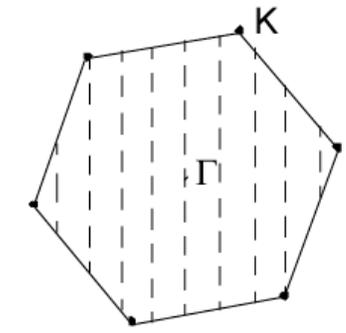
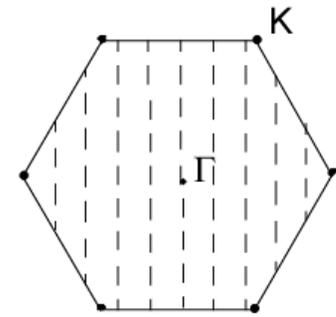
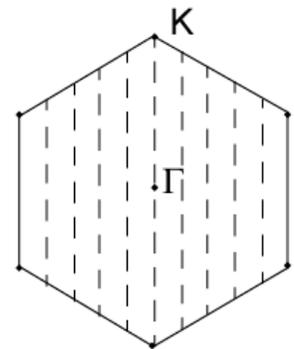


The (m,n) wrapping specifies a translation vector of the graphene lattice.

(5,5) Armchair Tube
Metal

(5,0) Zigzag Tube
Semiconductor

(5,-1) Tube
Metal
(small-gap SC)



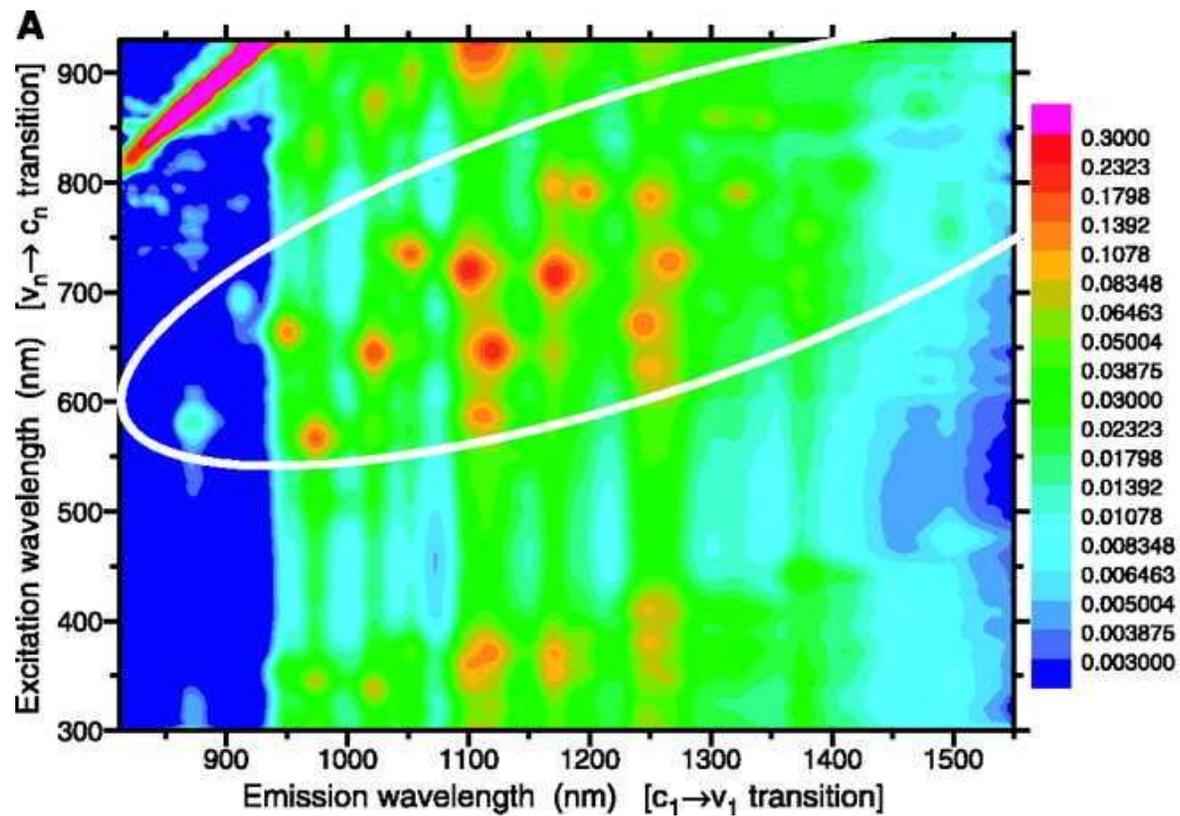
$m=n$

$\text{mod}(m-n,3) = \pm 1$

$\text{mod}(m-n,3) = 0, m \neq n$

Two Dimensional PLE Spectroscopy

Discrete Peaks are Excitations of Individual SWNT's



- **The Ratio Problem**

Anomalous scaling of gap ratios in large R limit

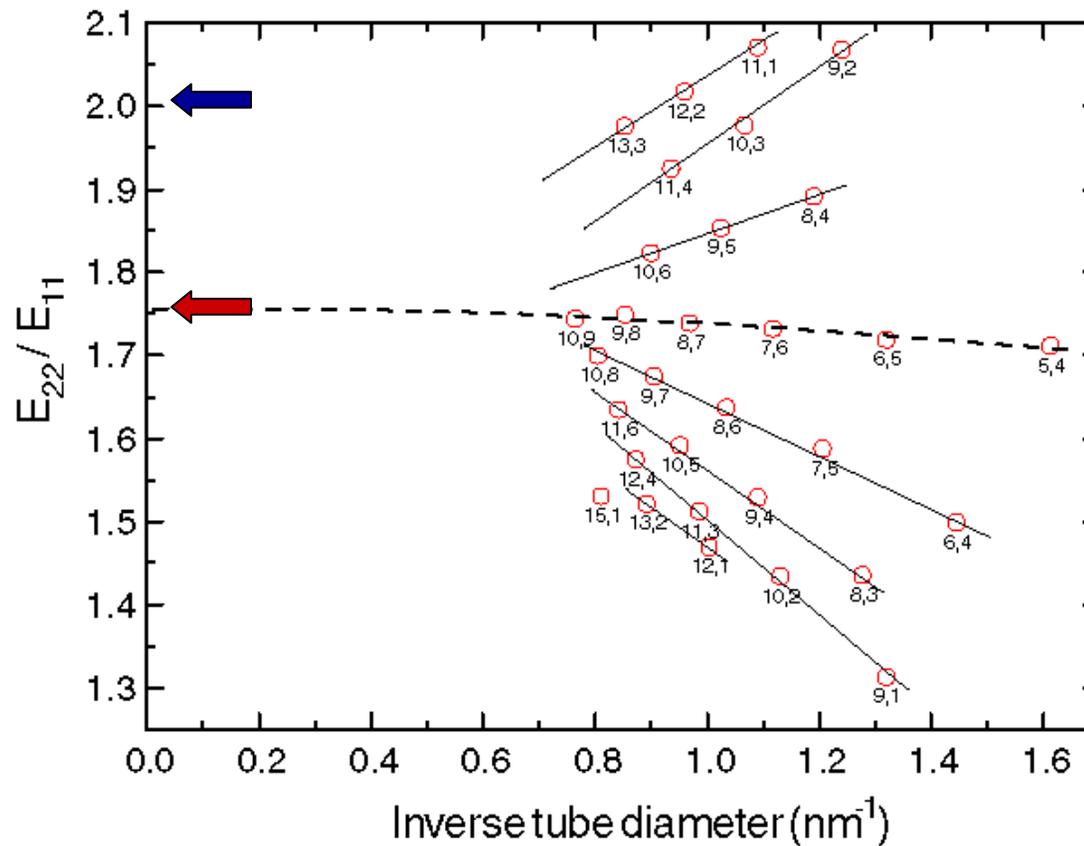
- **The Blue Shift Problem**

The observed gaps are blue shifted with nonlinear $1/R$ scaling

- **The Deviations Problem**

Anomalies in period-3 deviations from scaling

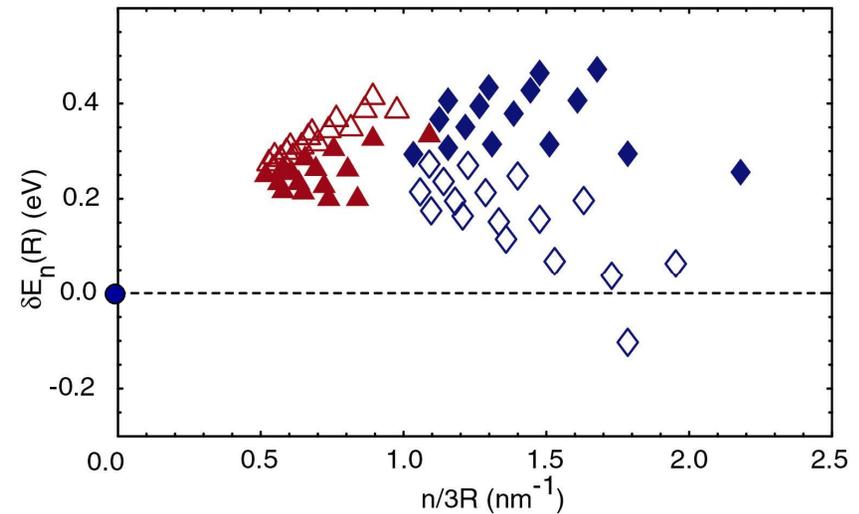
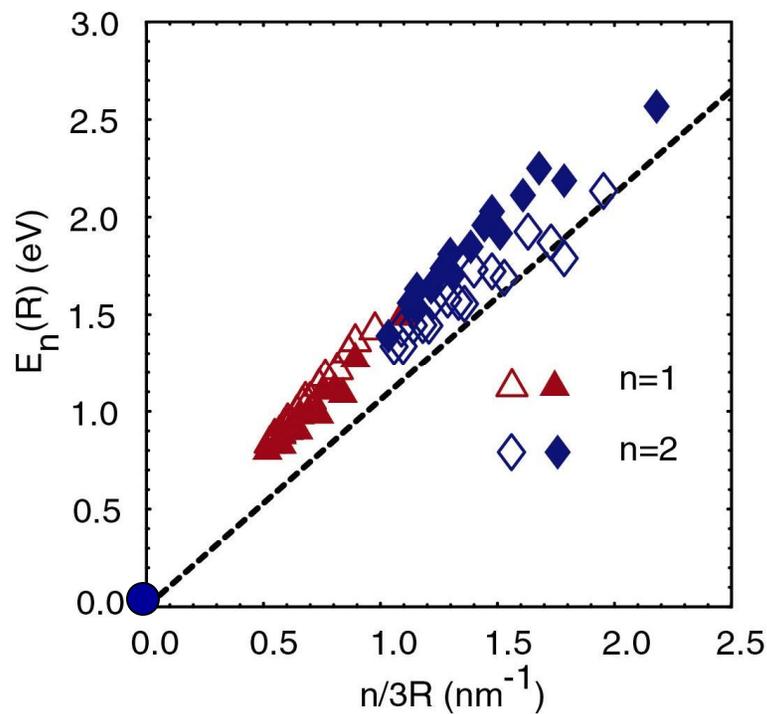
Ratio Problem: the ratio of absorption/emission frequencies < 2 in Large R Limit



Data: S.M. Bachilo et al. Science 298, 2361 (2002)

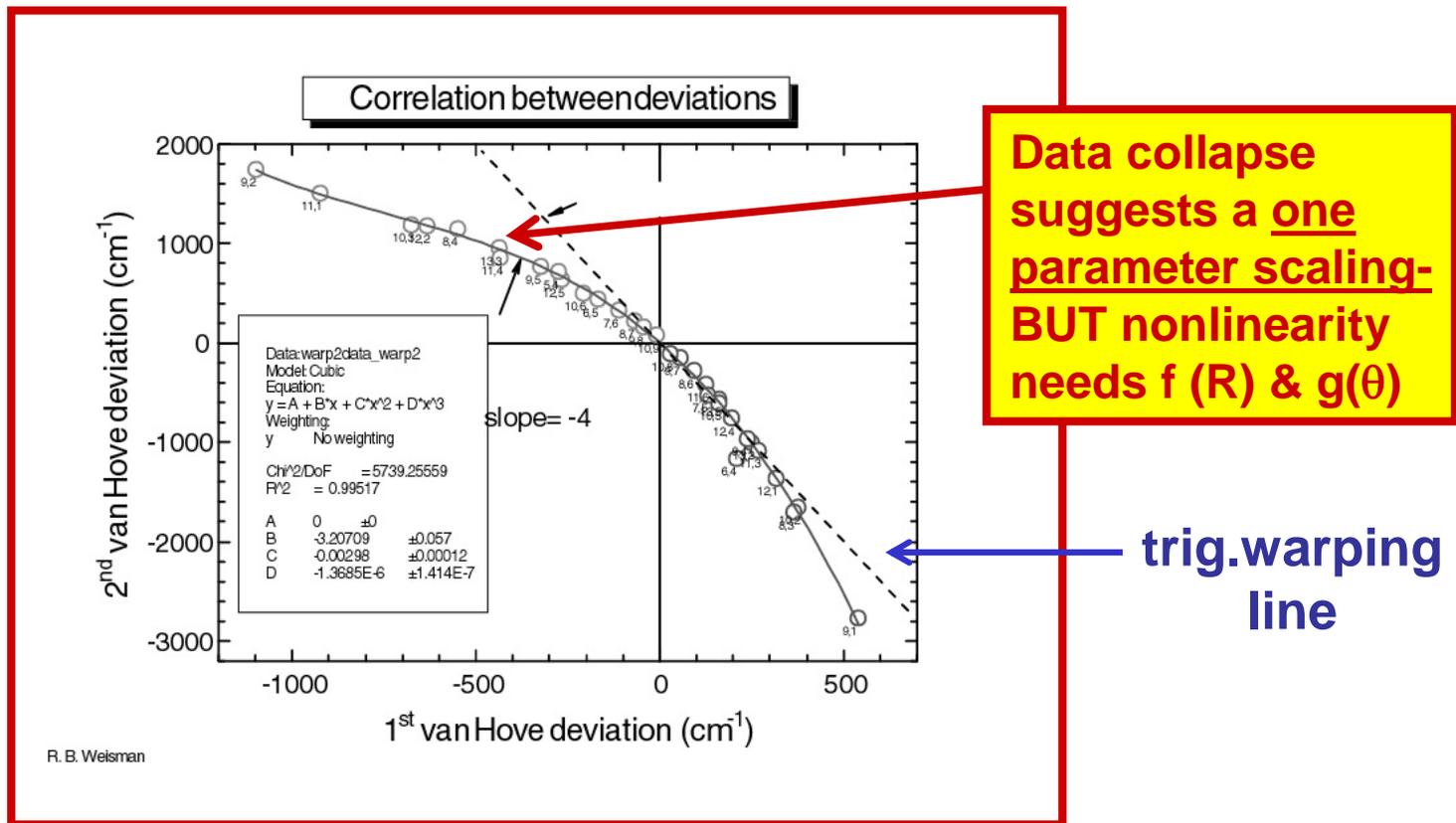
Blue Shift Problem: E_{11} and E_{22} are blue shifted wrt linearized theory

BUT with separatrix on single scaling curve (n/R)



(nearly armchair tubes at border)

Ratio Problem: Scaling of Deviations from Scaling
 (ref: *Structure Assigned Optical Spectra of Single Wall Carbon Nanotubes*,
 S. Bachilo et al., *Science* 298, 2361 (2002))



(This is still a puzzle..band effects? interactions? multiplet effects?)

Electron-Electron Interactions
are responsible for all three anomalies



NT Exciton Effects are Large

(binding energies are a substantial fraction of bandgap)

***Absorption/Fluorescence Frequencies Scale
in a Simple Way with Inverse Tube Radius***

(but not in the simplest way)

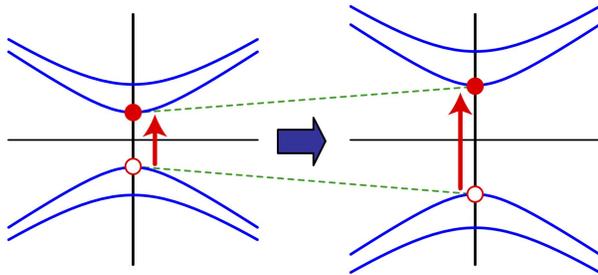
Separate 1D and 2D Interaction Effects

(the NT is actually a 2D structure)

Rule 1 There are competing interaction effects

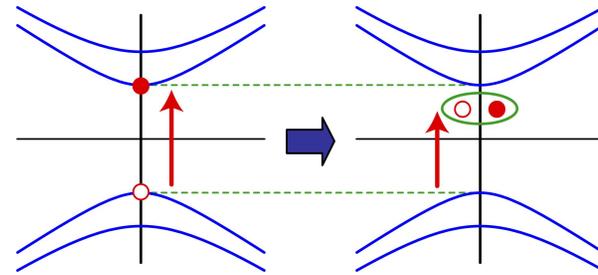
Coulomb Interaction gives a positive self energy...

exchange increases the observed gap



... and an attractive e-h interaction:

with particle-hole bound state at lower energy



Both effects are strong in NT's but subtle since they partially compensate

**Rule 2 The tube radius sets a fundamental length scale:
separation of 1D and 2D interaction effects**

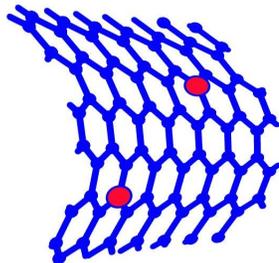
$$V(r) = \frac{e^2}{r} = V_{\text{long}}(r) + V_{\text{short}}(r)$$

Long Range Interaction : ($r > 2\pi R$)



**One Dimensional
Unscreened for large separation**

Short Range Interaction : ($a < r < 2\pi R$)



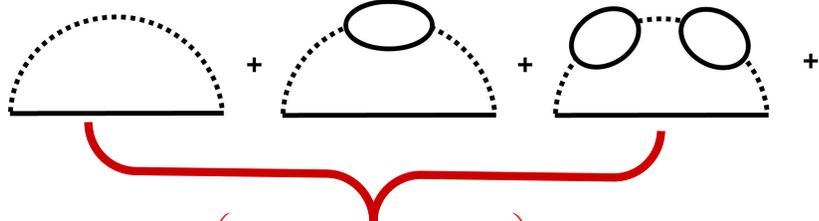
Two Dimensional

**Leads to nonlinear $q \log q$ shift in dispersion of
graphene, and nonlinearity in $E_{nn}(1/R)$**

Interactions renormalize quasiparticle dispersion $E(q)$ of two dimensional graphene

Noninteracting: $E(q) = \hbar v_F q + O(1/R^2)$

Interacting:



$$E(q) = \hbar v_F q \left(1 + \frac{g}{4} \log\left(\frac{\Lambda}{q}\right) \right) + O(1/R^2);$$

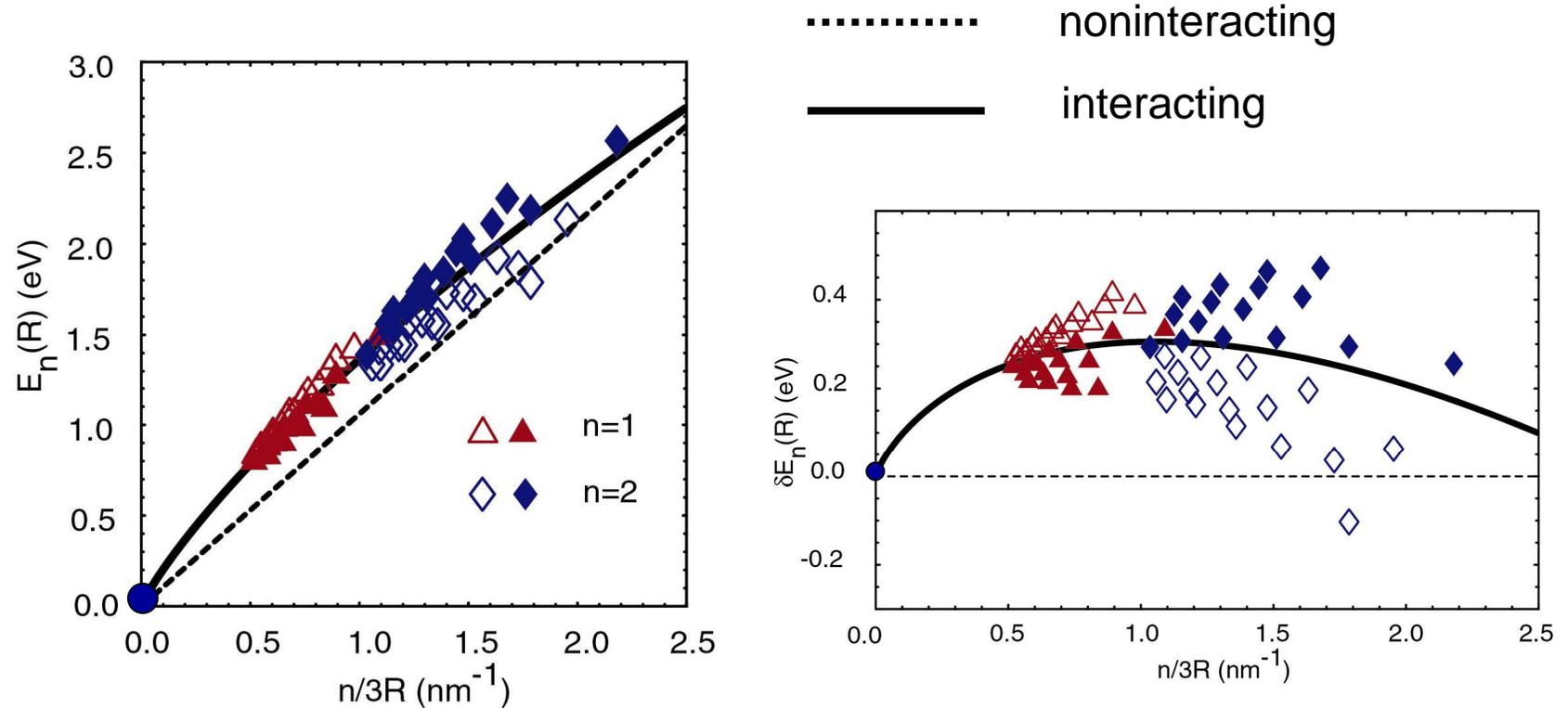
$$g = \frac{e^2}{\hbar v_F}$$

This is exact for $q \rightarrow 0$, with a scale dependent v_F and g :

(scales to perturbative regime at small q)

**Earlier work: J. Gonzalez, F. Guinea and M.A.H. Vozmediano
Phys. Rev. B 62, 4273 (2002)**

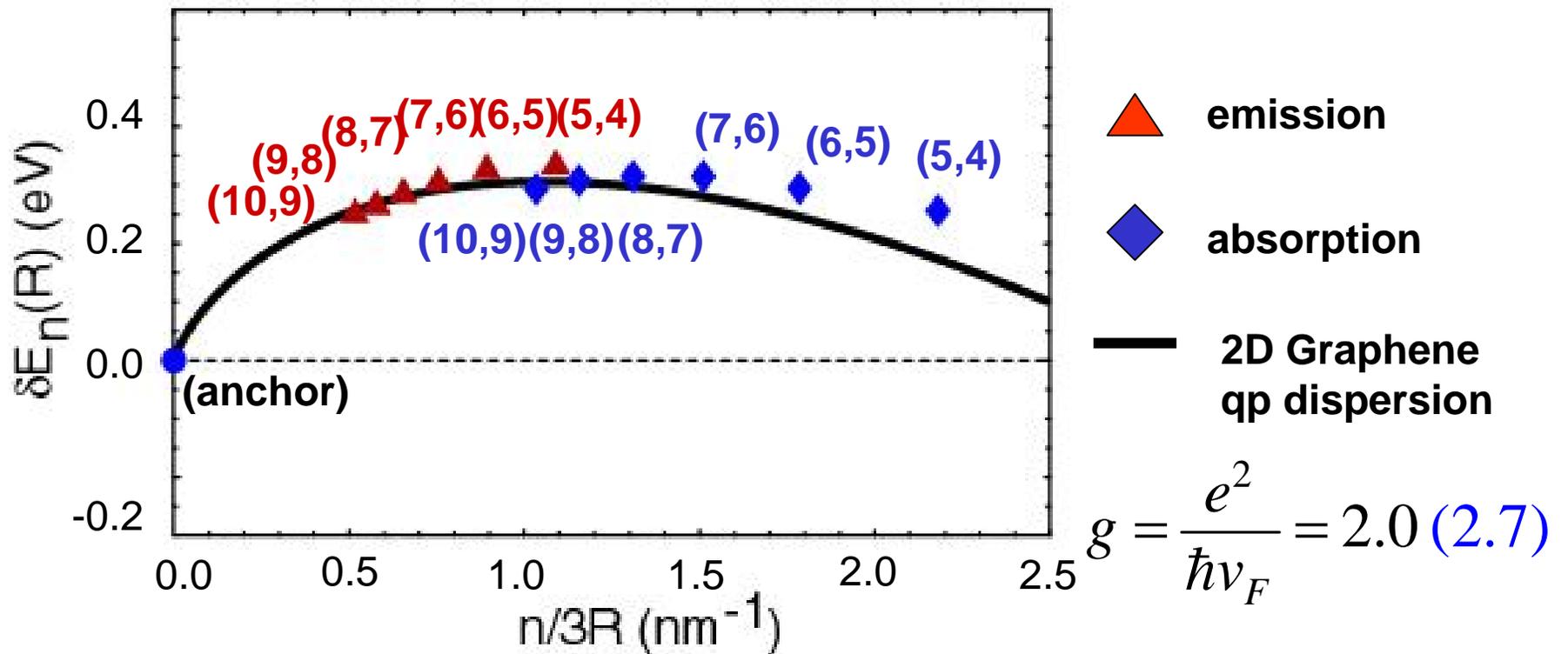
Map graphene quasiparticle energies to nanotube



***Resolves (by unifying!) ratio problem
and blue shift problem***



sin(3θ) Effects Are Small Near The Armchair Structures



But how would (could) this survive with even stronger 1D interaction effects



Rule 3. The long(est) range effects nearly balance each other

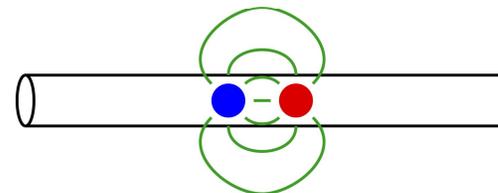
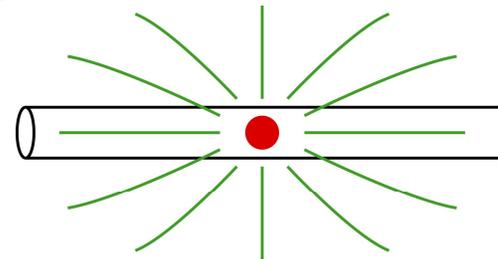
$$V(r) = \frac{e^2}{r} = V_{\text{long}}(r) + V_{\text{short}}(r)$$

schematically for $r > 2\pi R$

One Dimensional
(unscreened at large r)

Renormalizes the Band Gap

Binds the Exciton



An Exactly Solvable Model: Infinite Range Interaction

e.g. simplest model of a “quantum dot”

Bare Gap: 2Δ **Interaction Energy:** $V_0 N^2/2$

Quasiparticle Gap:

$$E(N+1) + E(N-1) - 2E(N) = 2\Delta + V_0$$


$$\textcircled{N+1} + \textcircled{N-1} - 2 \textcircled{N}$$

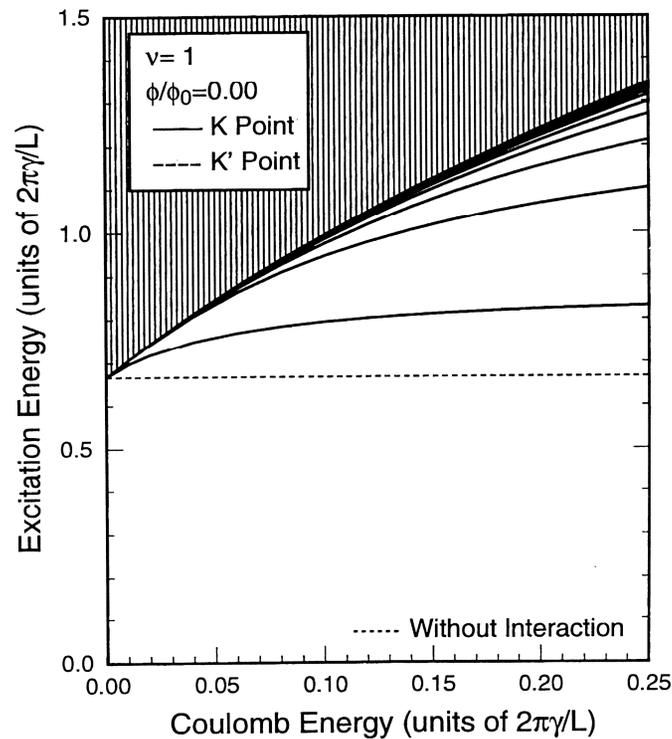
Electron-Hole Gap: 2Δ


$$\textcircled{e-h}$$

Near Cancellation for Screened NT Interaction

T. Ando, J. Phys. Soc. Japan 66,1066 (1997)

Numerical Calculation in Screened Hartree Fock Approximation



← Quasiparticle gap

← Lowest Exciton

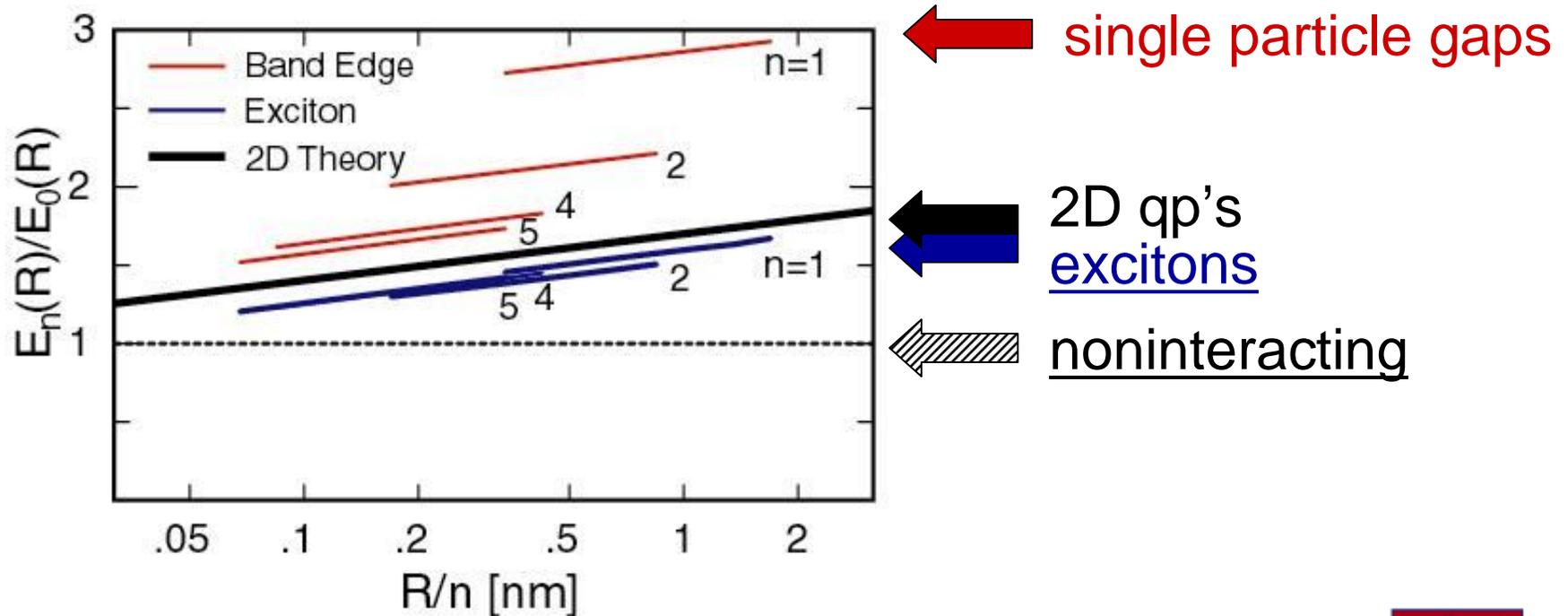
← Noninteracting

Interaction strength



Size-Scaling of Single Particle and Particle - Hole Energies

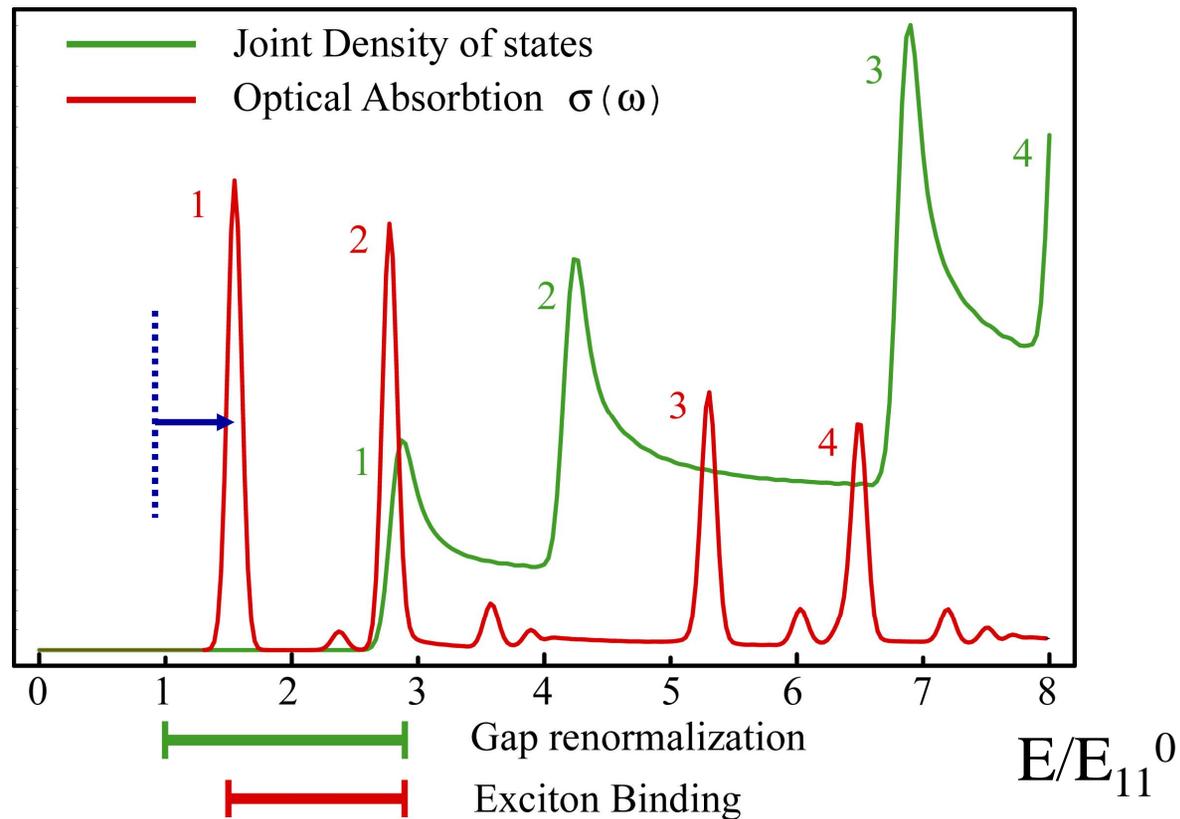
*C.L. Kane and EJM (PRL 93, 197402 (2004))
multiband mixing with screened interaction*



(Logarithm of tube radius)



Excitonic v. Interband Spectra



Oscillator strength in bound state

Suppress continuum van Hove singularity

Bandgap renormalization nearly cancelled by exciton binding.

Properties of NT Excitons

They are strongly bound

size ~ few tube radii, $\Delta E/E \sim 30\%$! Nearly all spectral weight in bound state

they carry spin (0,1) and valley (K,K') indices

these degeneracies are lifted by intervalley and exchange

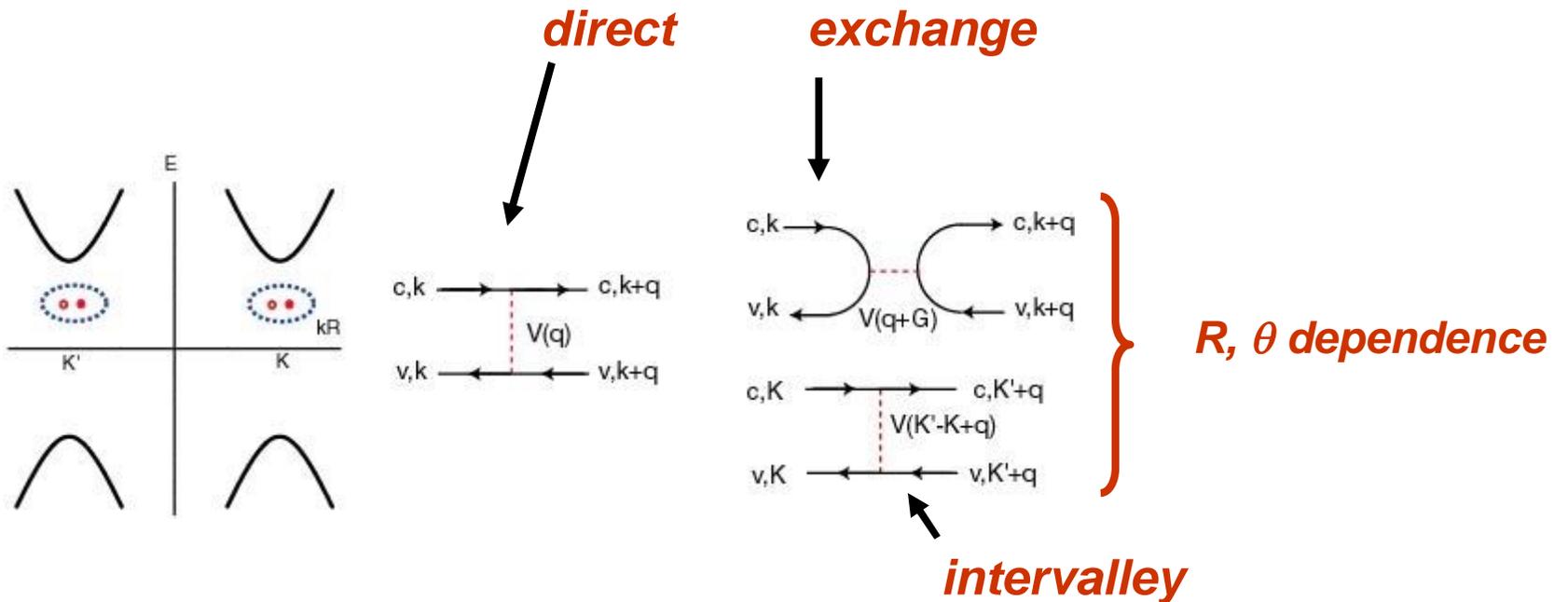
→ spectrum of dipole allowed and dark (forbidden) states

possibly stable to high density (?)

power law decay of transient absorption

→ long lived diffusing species

Spin and Valley Degeneracies Broken by Interactions



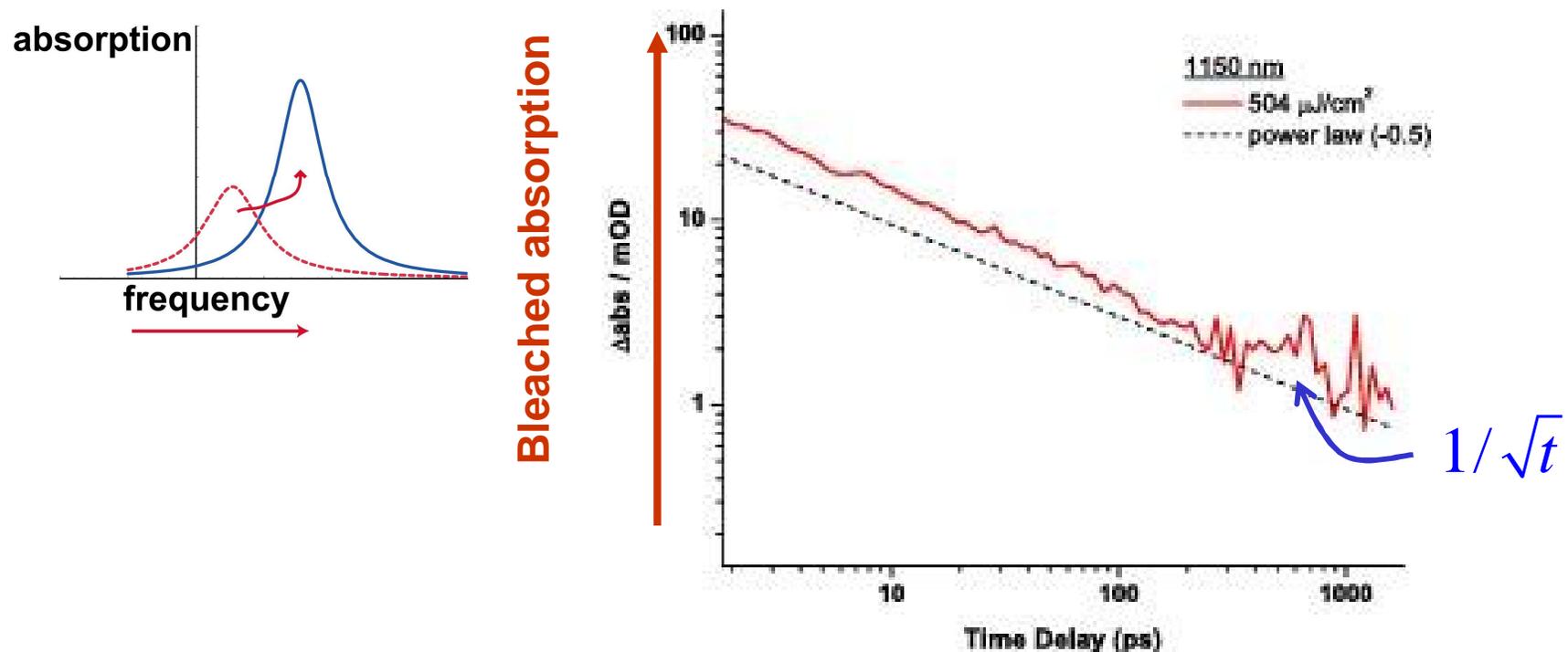
Exchange and Intervalley at finite momenta (θ –dependent)

Low Energy Triplet & “Dark” Singlet Excitons

Time Resolved Photo-Absorption Spectroscopy

R. Russo, EJM, CLK, D.E. Luzzi, I.B. Rubstov and M.J. Therien

Physical Review B 74, (R) 041405 (2006)



Power law decay of PA from a long lived
diffusive but nonemissive excited state



Conclusions...

Large NT Excitonic/Interaction Effects

Anomalies From “2D” Graphene Self Energy
(nontrivial scaling with inverse tube radius)

... and Questions

Why are comparable qp effects “missing” in STS?

Modification by multiplet effects, and 3θ dependence?

***Scale of extrinsic effects: dielectric environment,
doped carrier density...***

Collaborators

Charlie Kane (theory)

**Dave Luzzi, Rich Russo
Mike Therien, Igor Rubstov**

**Dina Zhabinskaya
Jesse Kinder**

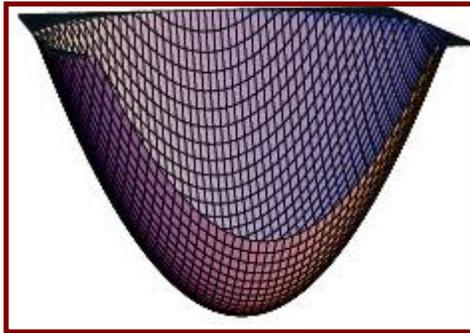
Bruce Weisman (Rice)

Univ. of Penn.

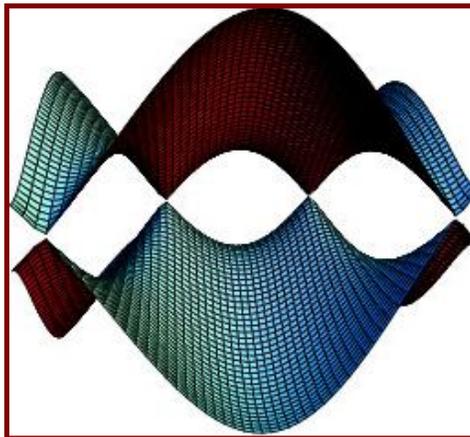
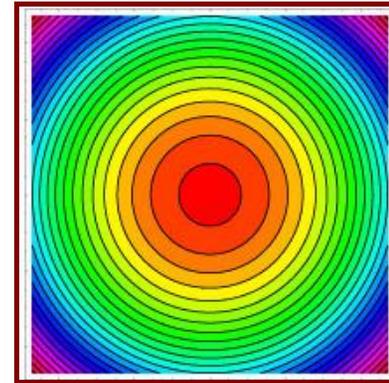
**Physics
Chemistry
Mat. Science**



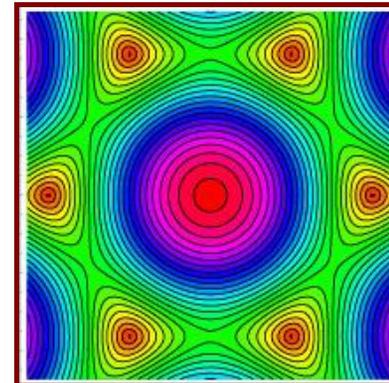
Graphene has a critical electronic state



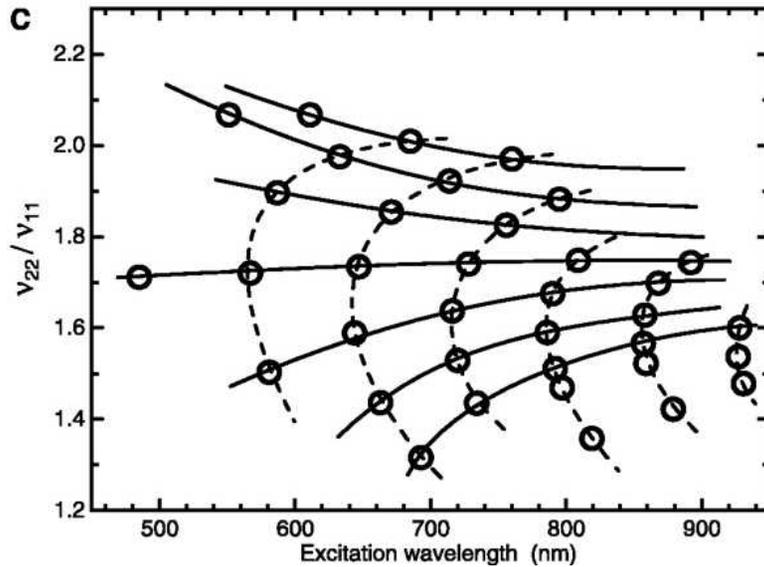
Dispersion of a
free particle in 2D..



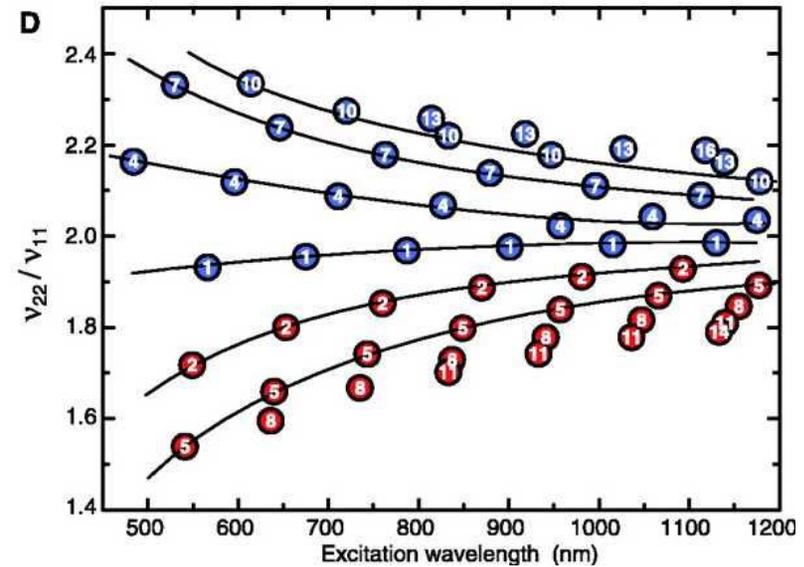
...is replaced
by an unconventional
 $E(k)$ relation on the
graphene lattice



Experimental “Ratio Plot”



Theory (Reich, 00)



By comparing the distributions of gap ratios the (n_1, n_2) values (hence R and θ) for each peak are assigned.

Corroborated by Raman spectroscopy of the radial breathing mode.

- **The Ratio Problem**

Anomalous scaling of gap ratios in large R limit

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Deviations Problem

(ref: *Structure Assigned Optical Spectra of Single Wall Carbon Nanotubes*, S. Bachilo et al., *Science* 298, 2361 (2002))

