

1D Exciton Diffusion on Semiconducting Nanotubes Using Photoabsorption Spectroscopy

R.M. Russo, D.E. Luzzi and E.J. Mele

Power law population relaxation ($\propto 1/\sqrt{t}$)

***History dependence of PA Lineshape*
⇒ exciton confinement energy**



Experimental

HipCO Tubes dissolved in 2% SDBS solution and purified

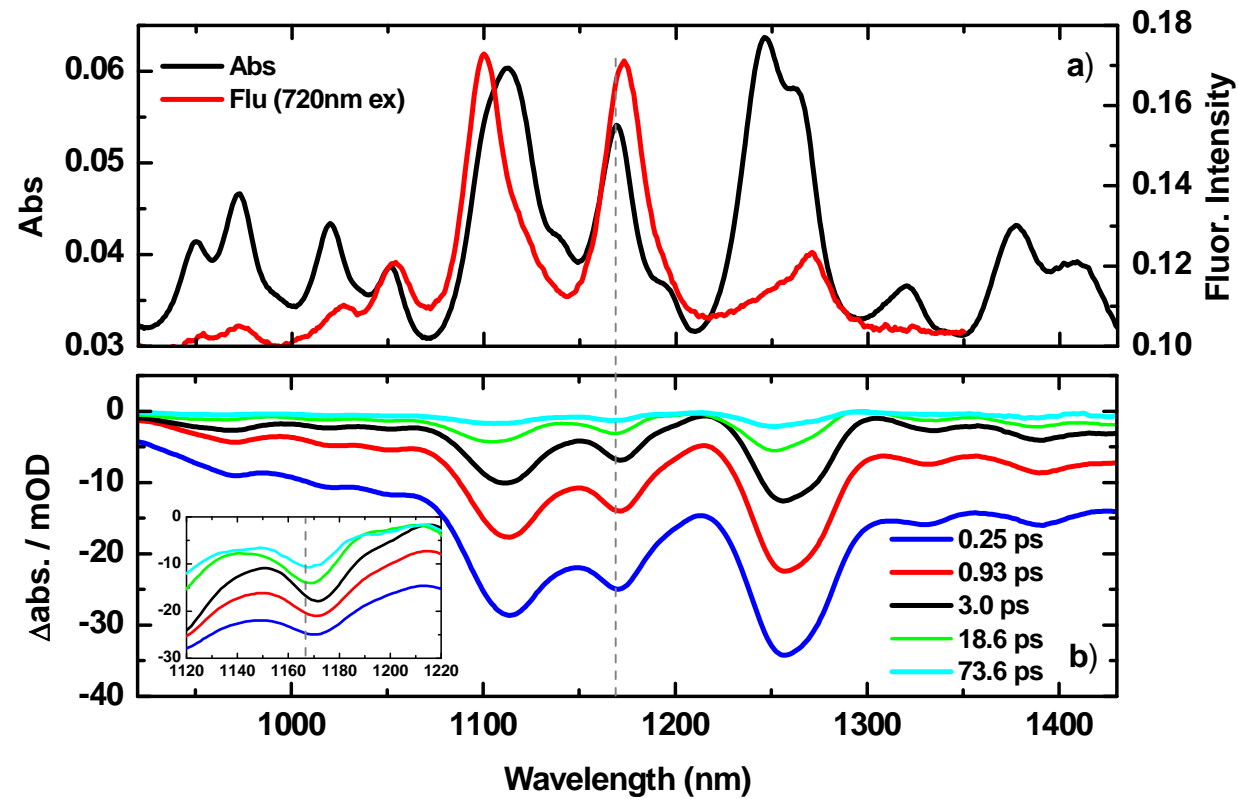
Pump: 0.1-1.0 mJ/cm² @ 725 nm

0.1-0.5 mJ/cm² @ 670 nm

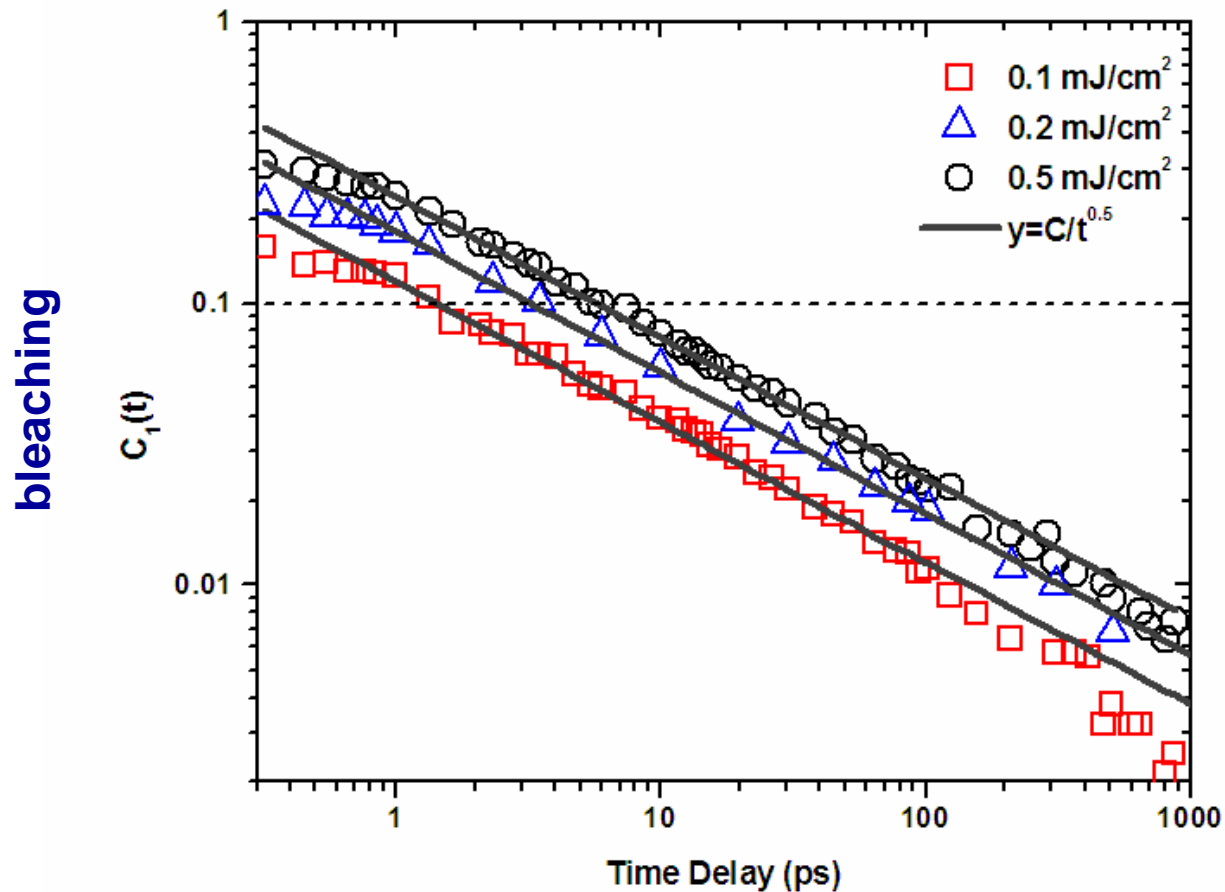
Probe: S₁₁ absorption from 920-1430 nm;

0.2 ps < t < 120 ps

Measure $\Delta\alpha(\lambda, t)$ after primary excitation

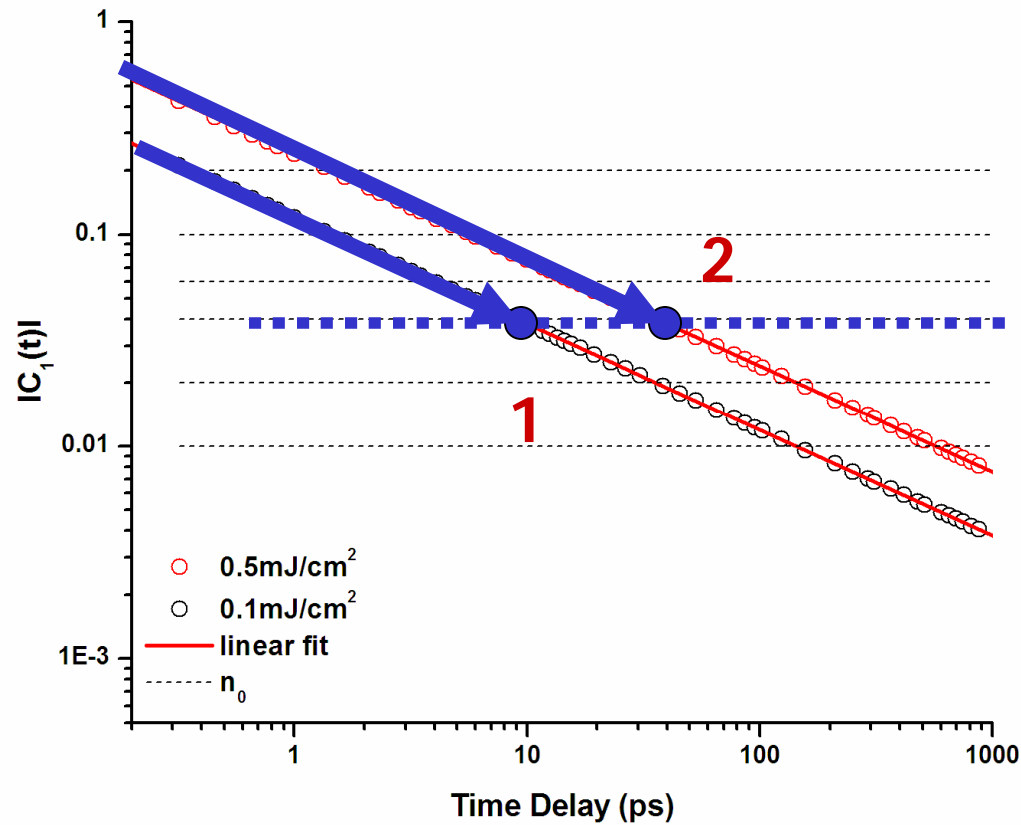


Power Law Relaxation of Excited Population



R.M Russo et al. Phys. Rev. B 74, R041405 (2006)

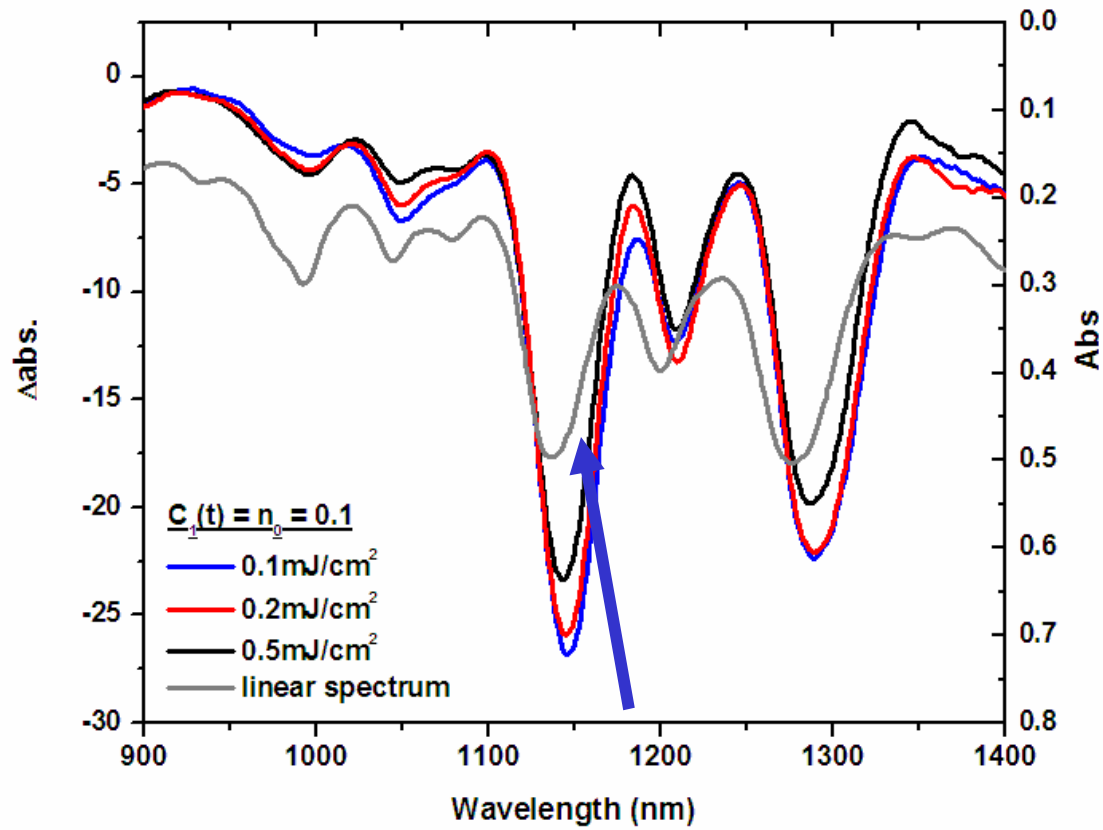
For two systems evolved to same density



$$\frac{\dot{n}_1}{\dot{n}_2} > 1$$

system evolved from the higher density is the "slower"

For two systems that evolve to same density

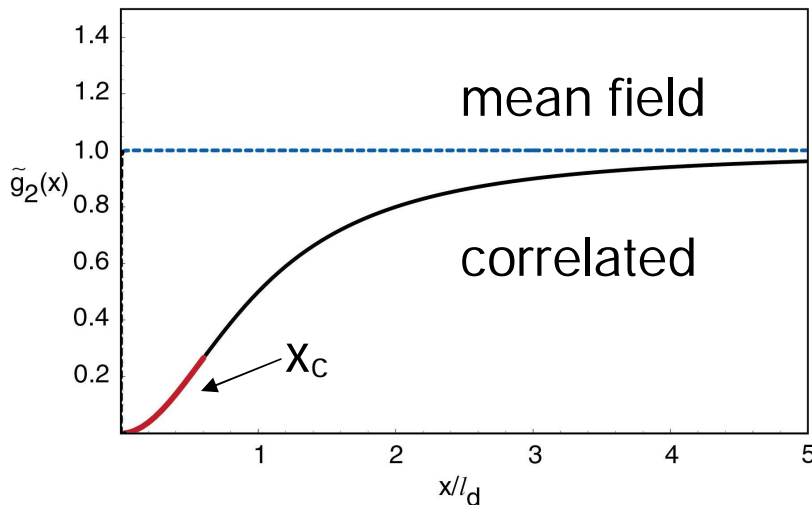


.. and its bleaching spectrum is shifted
"history dependence"

Diffusion Limited Pair Annihilation

In mean field theory: $\frac{dn}{dt} = -Cn^2$

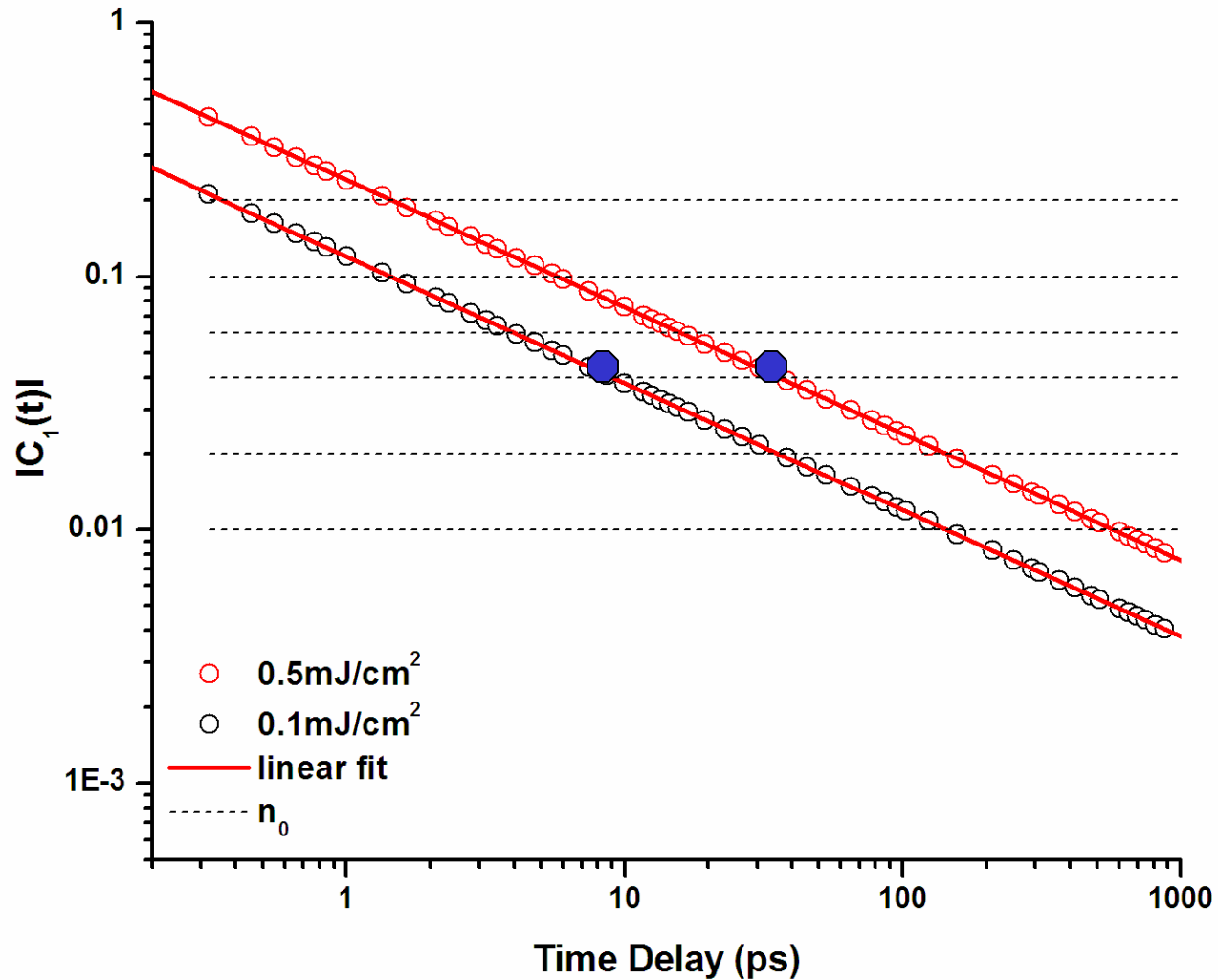
but in a correlated distribution: $\frac{dn}{dt} = -C \times \tilde{g}_2(x_c, t) \times n^2$



e.g:

$$g_2(x, t) = \frac{x^2}{x^2 + Dt}$$

Relate the Relaxation Rates

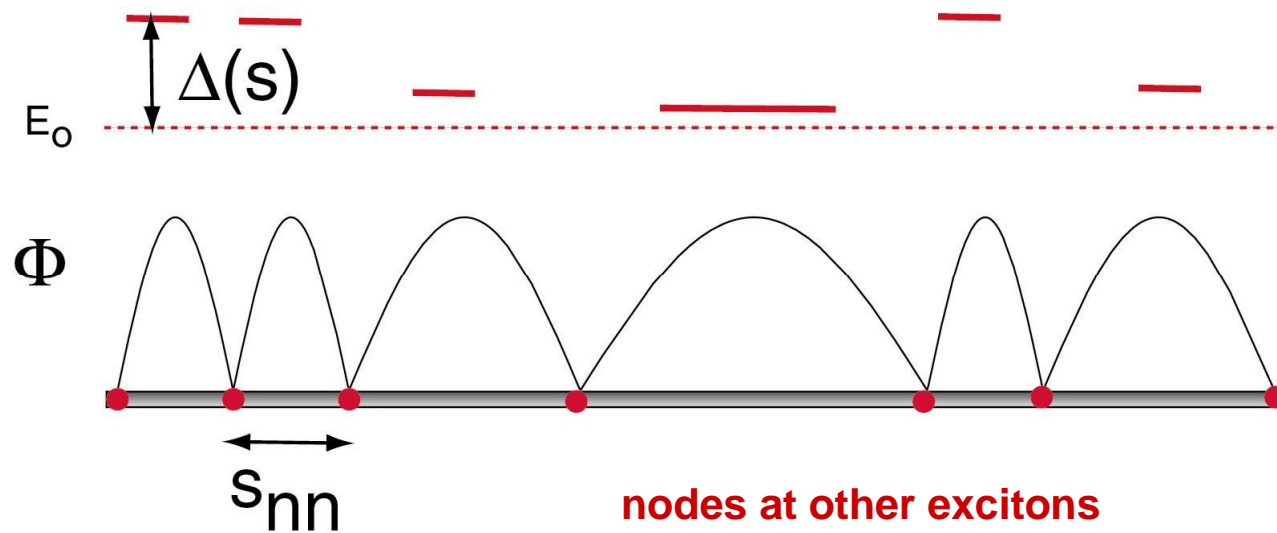


$$\frac{\dot{n}_1}{\dot{n}_2} = \frac{\tilde{g}_2(x_c, t_1)}{\tilde{g}_2(x_c, t_2)}$$

for $x_c \ll \ell_d$

$$\approx \frac{x_c^2 / Dt_1}{x_c^2 / Dt_2} = \frac{t_2}{t_1}$$

Frequency Shifts from Exciton Confinement Energy



Lineshape from distribution of nn spacings

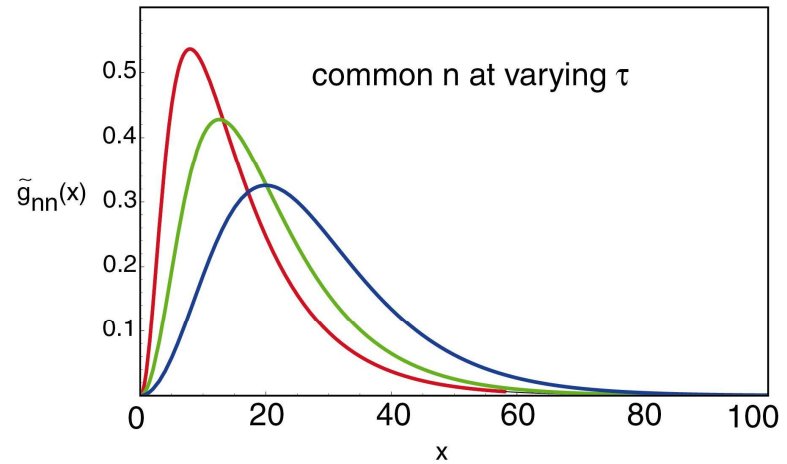
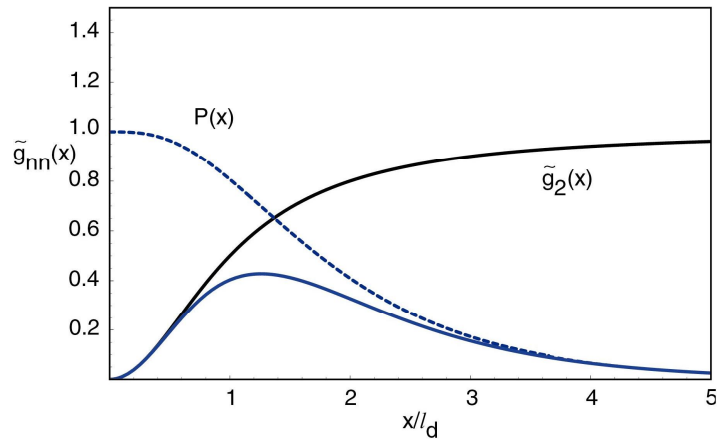
Time evolution of distribution of nn spacings

$$g_{nn}(x) = n \times \tilde{g}_2(x/\ell) \times P(x,t); \ell = \sqrt{Dt}$$

Distribution of pair separations

Probability of first neighbor at range x

$$P(x,t) = \exp(-n(t)x + n(t)\ell \times \arctan(x/\ell))$$



Lineshape Calculation

Lineshape from ground state absorption

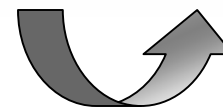
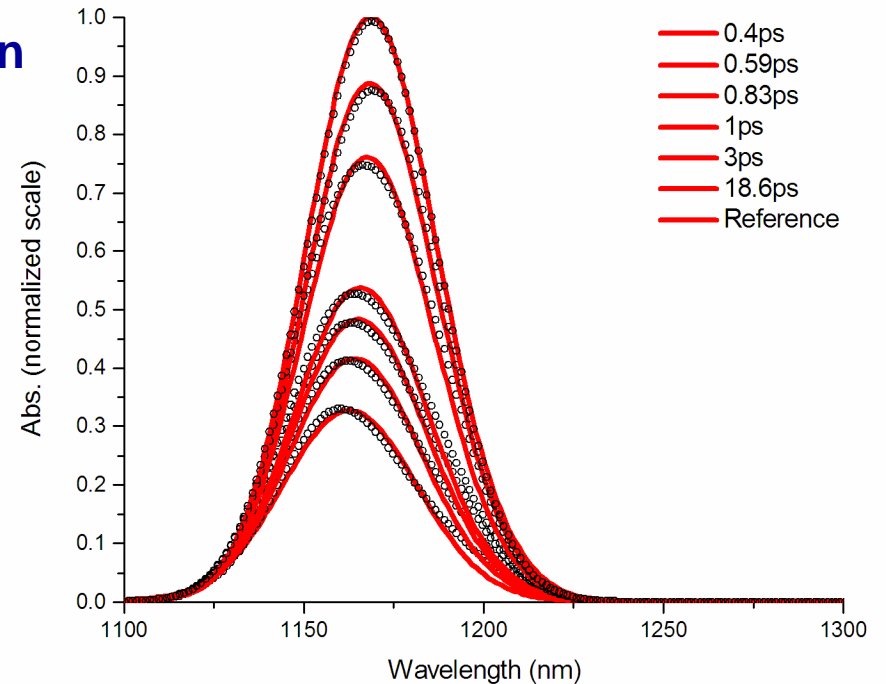
$$A(\omega, \omega_o) = L(\omega - \omega_o)$$

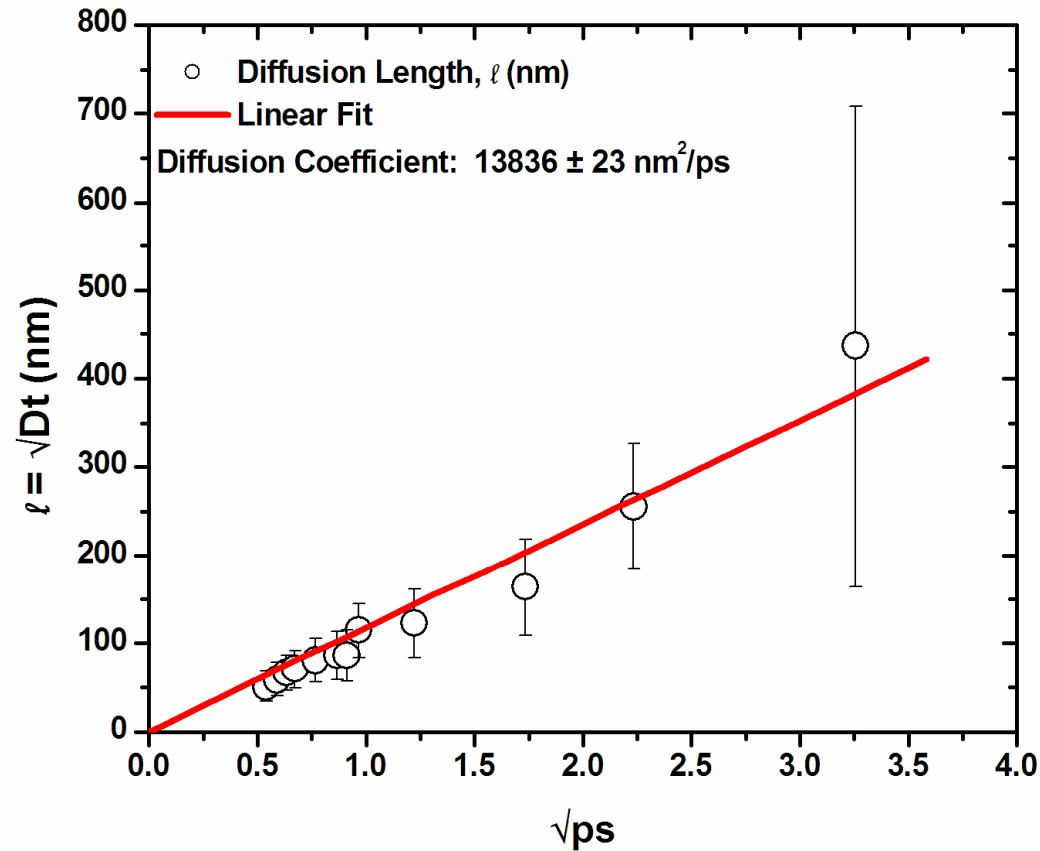
..shifted by the confinement energy

$$\omega_o \rightarrow \omega_o \left(1 + 2 \left(\frac{\pi \hbar v_F}{s E_o} \right)^2 \right)$$

.. and averaged over the nn distribution

$$\langle A(\omega) \rangle = \int_0^\infty L(\omega - \omega_o(s)) g_{nn}(s, t) \times \frac{s}{\sum s} ds$$





Best fit: $D=138 \pm 23 \text{ cm}^2/\text{sec}$

**Compare: Korovyanko et al. $D \sim 120 \text{ cm}^2/\text{sec}$ (PRL 92, 017403 (2004))
(from measurement of polarization memory)**

Further Comments

Pairwise recombination \Leftrightarrow triplet-triplet annihilation?

**Exciton density (alone) does not describe
short range correlations: population relaxation, PA...**

**Crossover from dense to dilute regime after first passage time
 $L^2/D \sim 100$ ps**



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